

AXIAL FLOW TURBOMACHINERY

Dr. János VAD

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1.1. Classification

Gas

(Liquid)

(Multiphase)

Power input

(Power output)

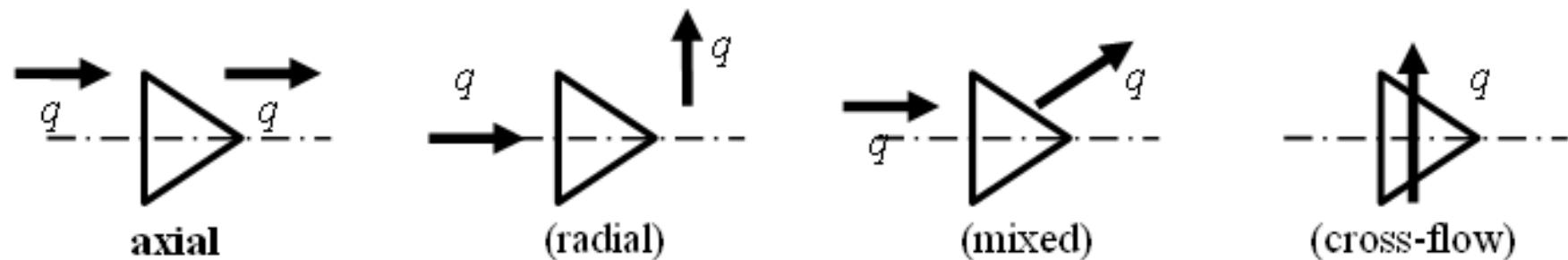
Principle:

Euler principle: TURBOMACHINERY

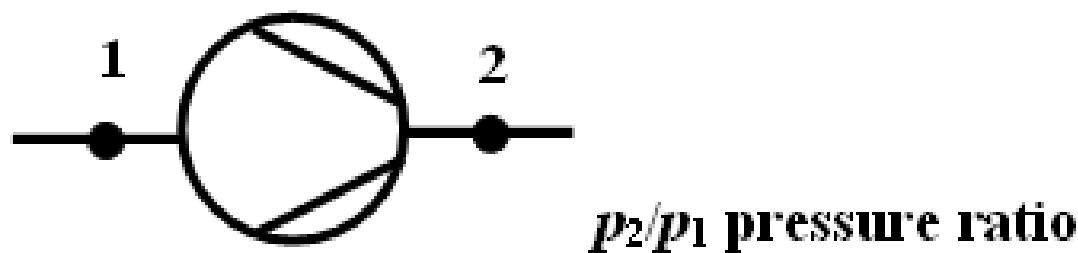
(Volumetric principle)

1.2. Classification of turbomachinery

Flow direction:



Pressure increase, pressure ratio:



A/ $p_2/p_1 < 1.1$ (1.2) fans

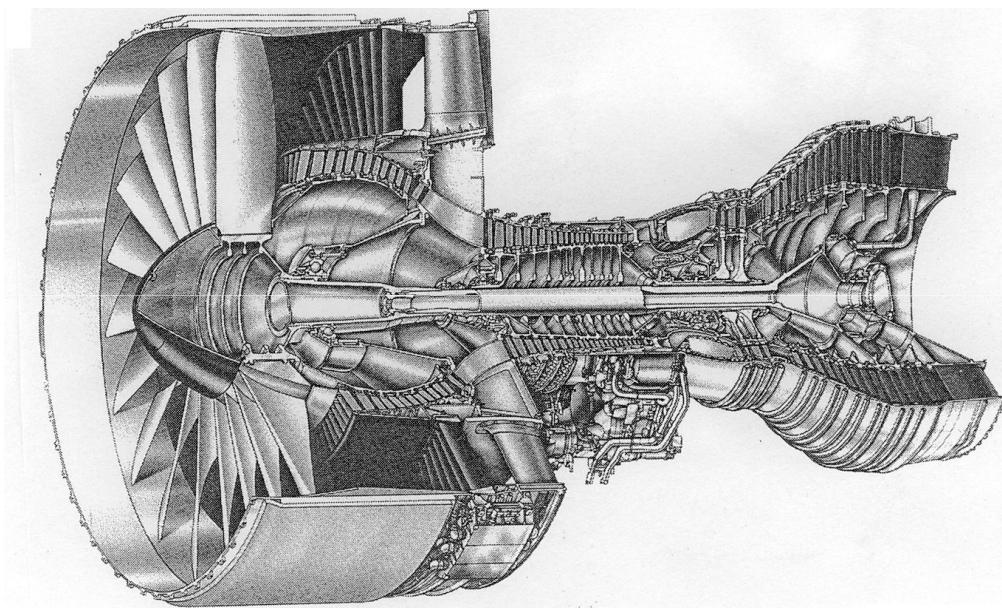
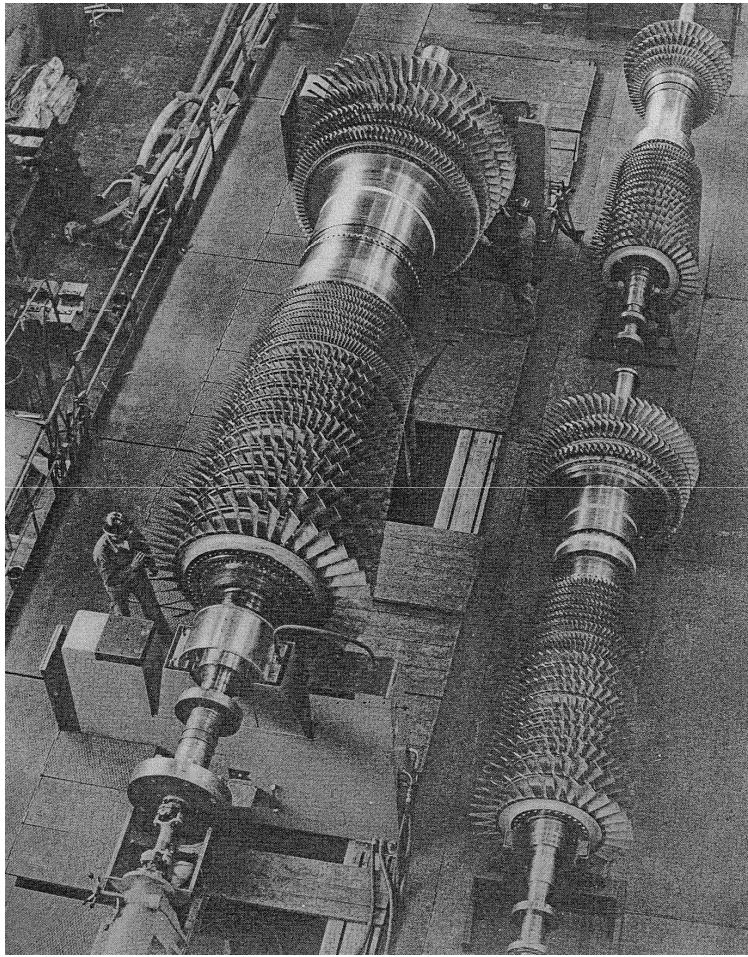
$\rho \approx \text{constant}$, $\Delta T \approx 0$

B/ $1.1 < p_2/p_1 < 3$ blowers

$\rho \neq \text{const}$, $\Delta T > 0$, *natural cooling*

C/ $3 < p_2/p_1$ compressors

$\rho \neq \text{const}$, $\Delta T \gg 0$, *artificial cooling*.



FANS:

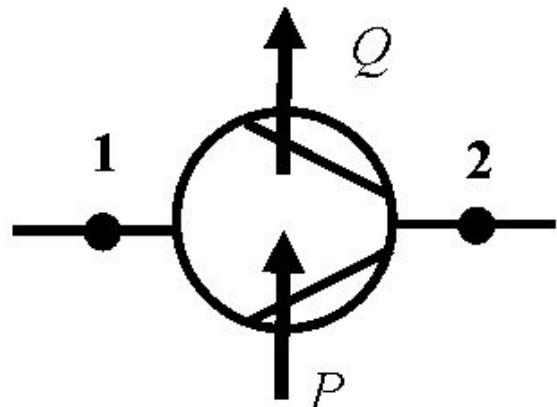
- Isentropic approach: $p_2/p_1 = (\rho_2/\rho_1)^\gamma$ $\frac{\rho_T}{\rho_s} = \left(\frac{T_T}{T_s}\right)^{\frac{1}{\gamma-1}}$
- If $p_2/p_1 = 1.1$, $\rho_2/\rho_1 = 1.07$
- Even more strict condition $|\rho_T - \rho_s| \leq 0.05\rho_s$
- Energy equation between S of suction side point and T of stagnation point of nose cone:

$$T_s + \frac{v_s^2}{2c_p} = T_s \left(1 + \frac{\chi R Ma_s^2}{2c_p} \right) = T_T \quad \text{Ma}_s < 0.31$$

Nearly atmospheric pressure on the suction side: $\Delta p < 0.1 \text{ bar}$

Circumferential speed of blade tip $< 100 \text{ m/s}$

1.3. Work process of fans



Ideal (inviscid) case:

$$\frac{P}{q_m} - \frac{Q}{q_m} = \left[\frac{v^2}{2} + gh + U + \frac{p}{\rho} \right]_1^2 = i_{t2} - i_{t1}$$

$Q = 0, \Delta U = 0, gh$ generally plays no role

$$P = q_m \left[\frac{v^2}{2} + \frac{p}{\rho} \right]_1^2 = q_v \left[\rho \frac{v^2}{2} + p \right]_1^2 = q_v \Delta p_{tid}$$

Euler equation of turbomachines:

$$\Delta p_{tid} = \rho(\underline{v}_2 \underline{u}_2 - \underline{v}_1 \underline{u}_1)$$

A/ Volumetric losses

$$P = q_{VR} \Delta p_{tid} \quad q_{VR} > q_V \quad \eta_V = q_V / q_{VR}$$

B/ Friction losses

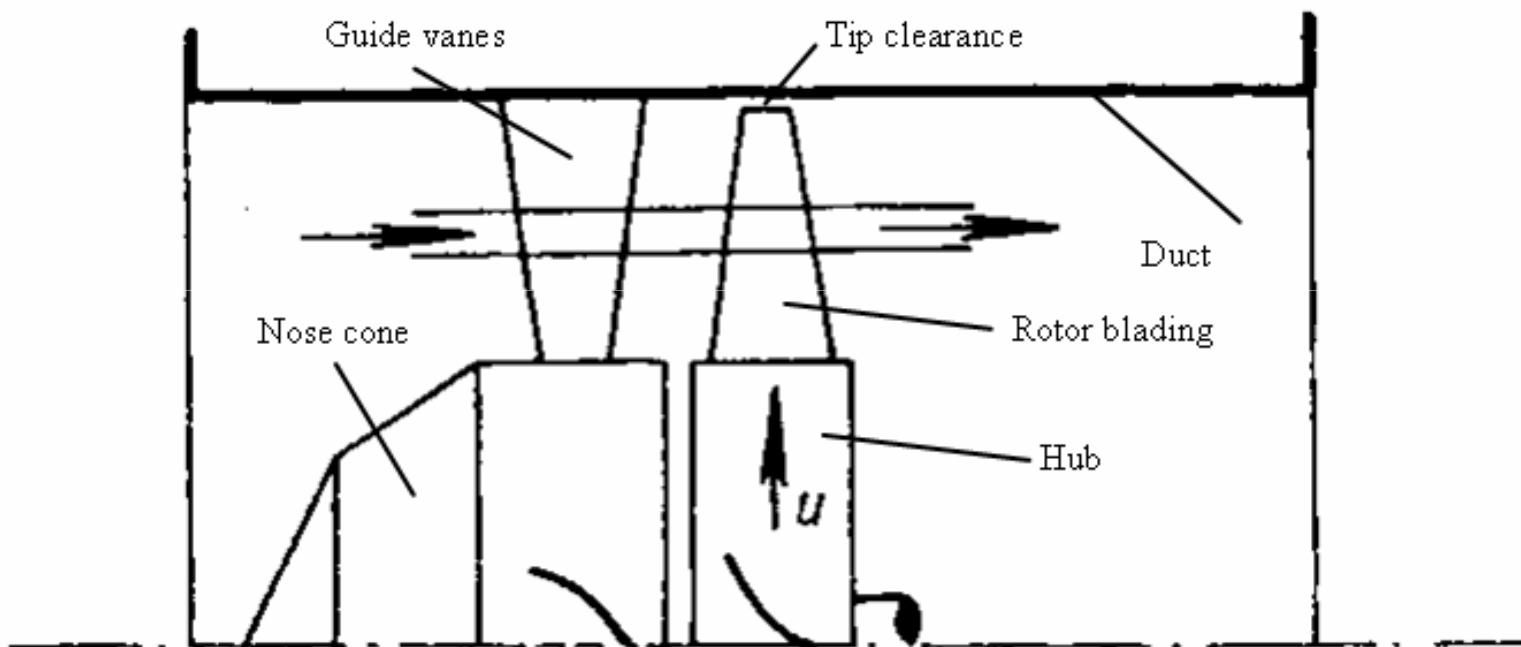
$$\eta_h = \Delta p_t / \Delta p_{tid} \quad P = q_{VR} \Delta p_{tid} = \frac{q_V}{\eta_V} \frac{\Delta p_t}{\eta_h} = \frac{P_{useful}}{\eta_V \eta_h}$$

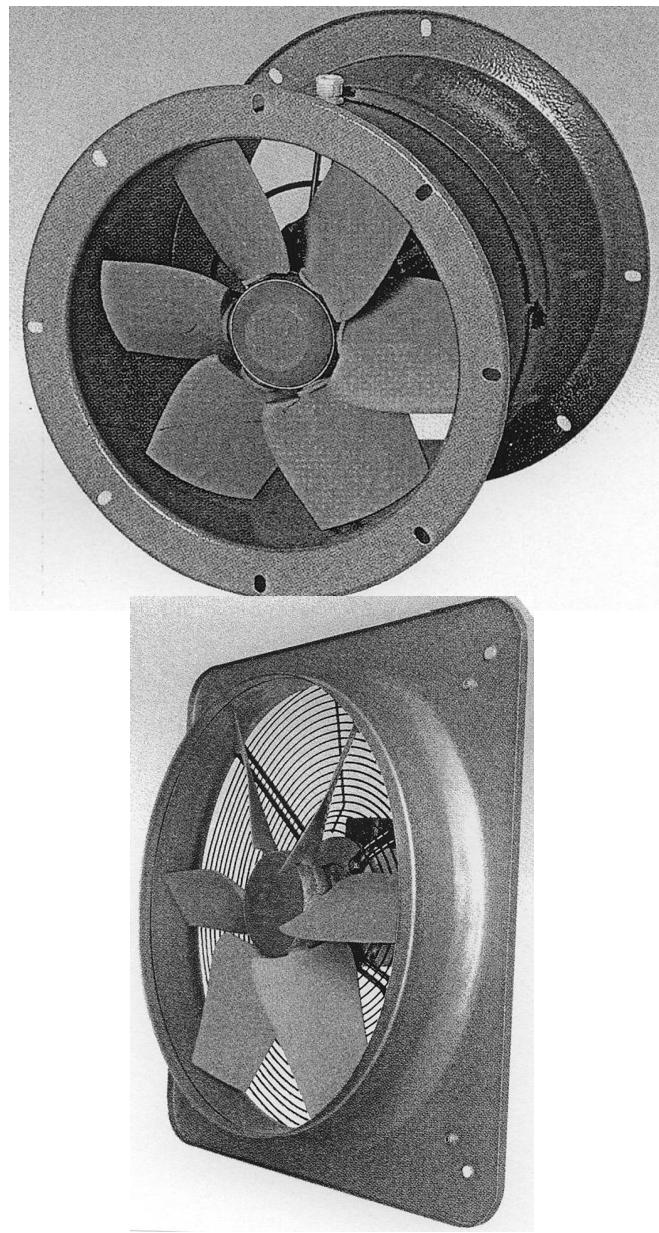
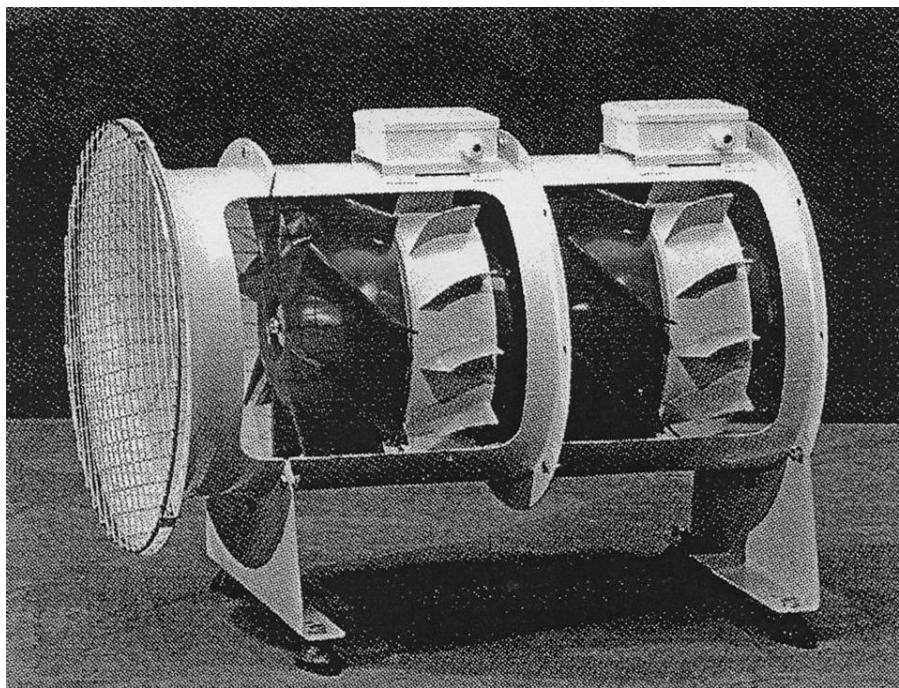
C/ Mechanical losses

$$\eta_m = P / P_{mechanical} \quad P_{overall} = \frac{P_{useful}}{\eta_V \eta_h \eta_m} = \frac{P_{useful}}{\eta_{overall}}$$

Fans: $\eta_m \approx 1$, $\eta_V \approx 1$, $\eta_{overall} \approx \eta_h$

1.5. Construction of axial fans



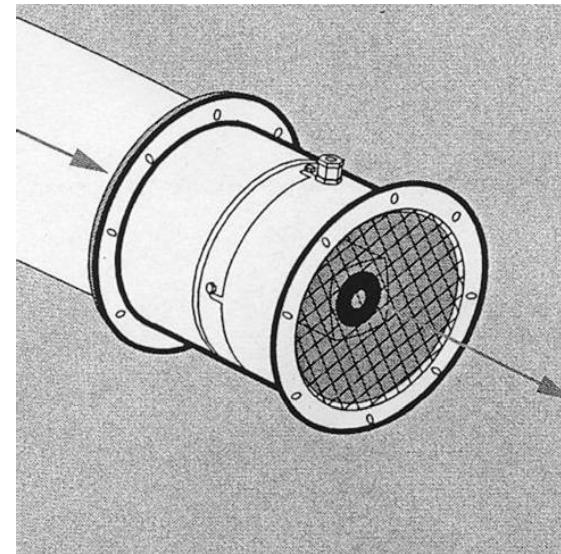
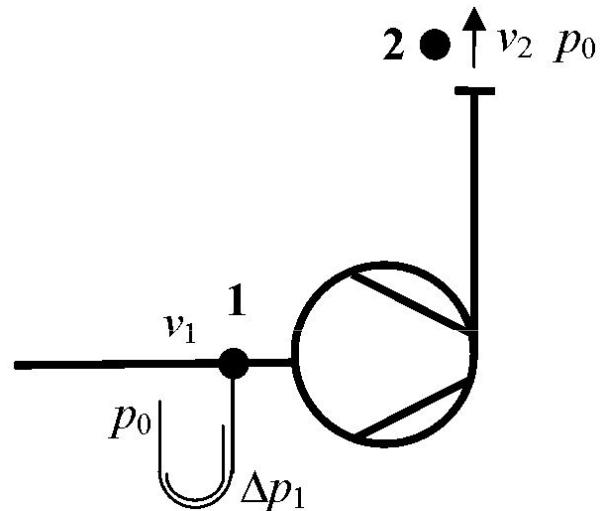


PRINCIPAL DIFFERENCES BETWEEN RADIAL AND AXIAL TURBOMACHINES:

- Axial turbomachinery: usually smaller total pressure rise
- Axial turbomachinery: usually higher volume flow rate
- Axial: moderate flow deflection: moderate fluid mechanical losses: higher stage efficiency
- Axial: moderate flow deflection in the connecting system: moderate system losses

1.6. Fan arrangements: technology- and geometry-dependent!

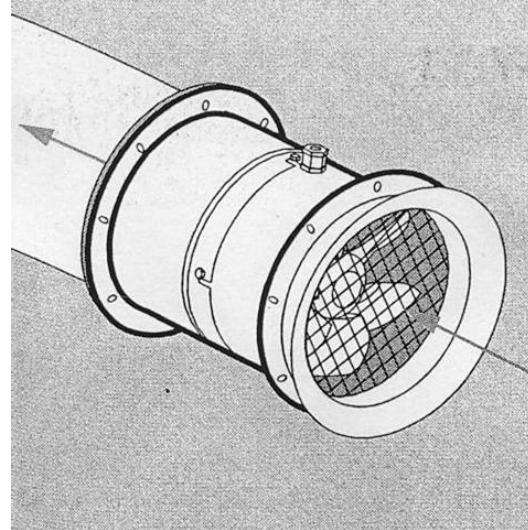
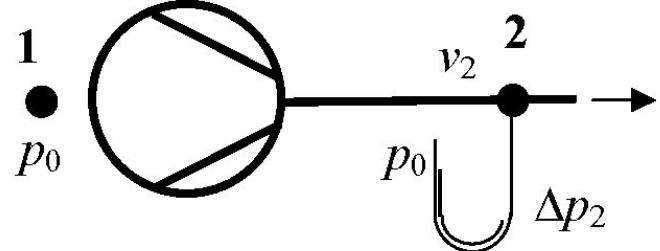
From the duct to the surroundings



$$\Delta p_t = \left(\rho \frac{v_2^2}{2} + p_0 \right) - \left[\rho \frac{v_1^2}{2} + (p_0 - \Delta p_1) \right] = \Delta p_1 + \rho \frac{v_2^2}{2} - \rho \frac{v_1^2}{2}$$

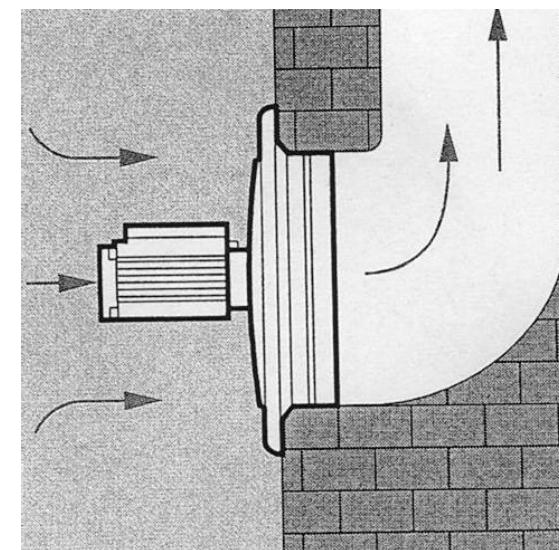
$$\Delta p_{st} = \Delta p_t - \rho \frac{v_2^2}{2} = \Delta p_1 - \rho \frac{v_1^2}{2}$$

From the surroundings to the duct

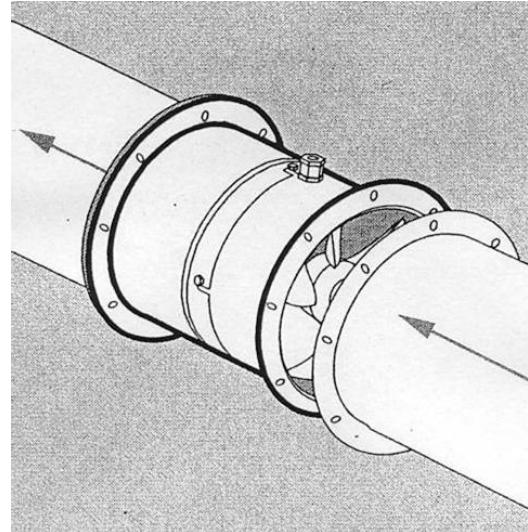
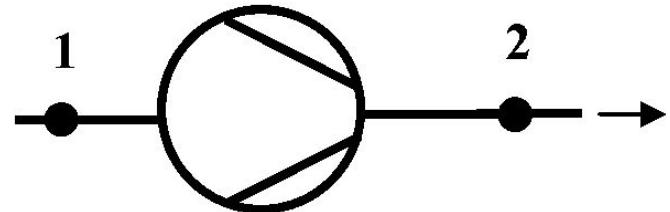


$$\Delta p_t = \left[\rho \frac{v_2^2}{2} + (p_0 + \Delta p_2) \right] - p_0 = \Delta p_2 + \rho \frac{v_2^2}{2}$$

$$\Delta p_{st} = \Delta p_2$$



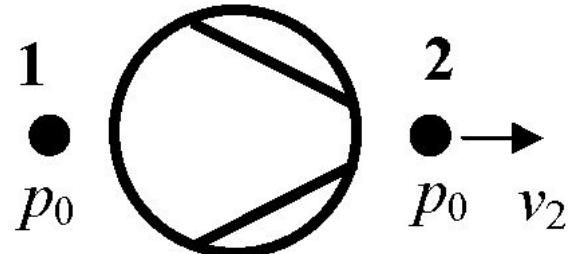
From duct to duct



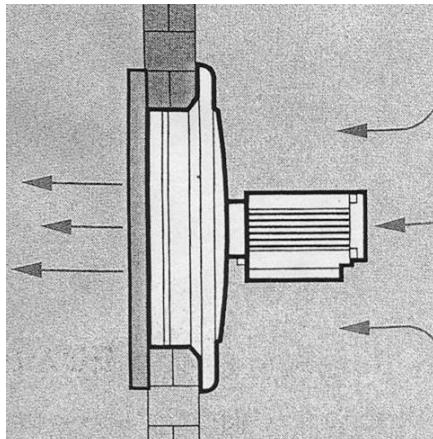
$$\Delta p_t = \left(\rho \frac{v_2^2}{2} + p_2 \right) - \left(\rho \frac{v_1^2}{2} + p_1 \right)$$

$$\Delta p_{st} = p_2 - \left(\rho \frac{v_1^2}{2} + p_1 \right)$$

From the surroundings to the surroundings

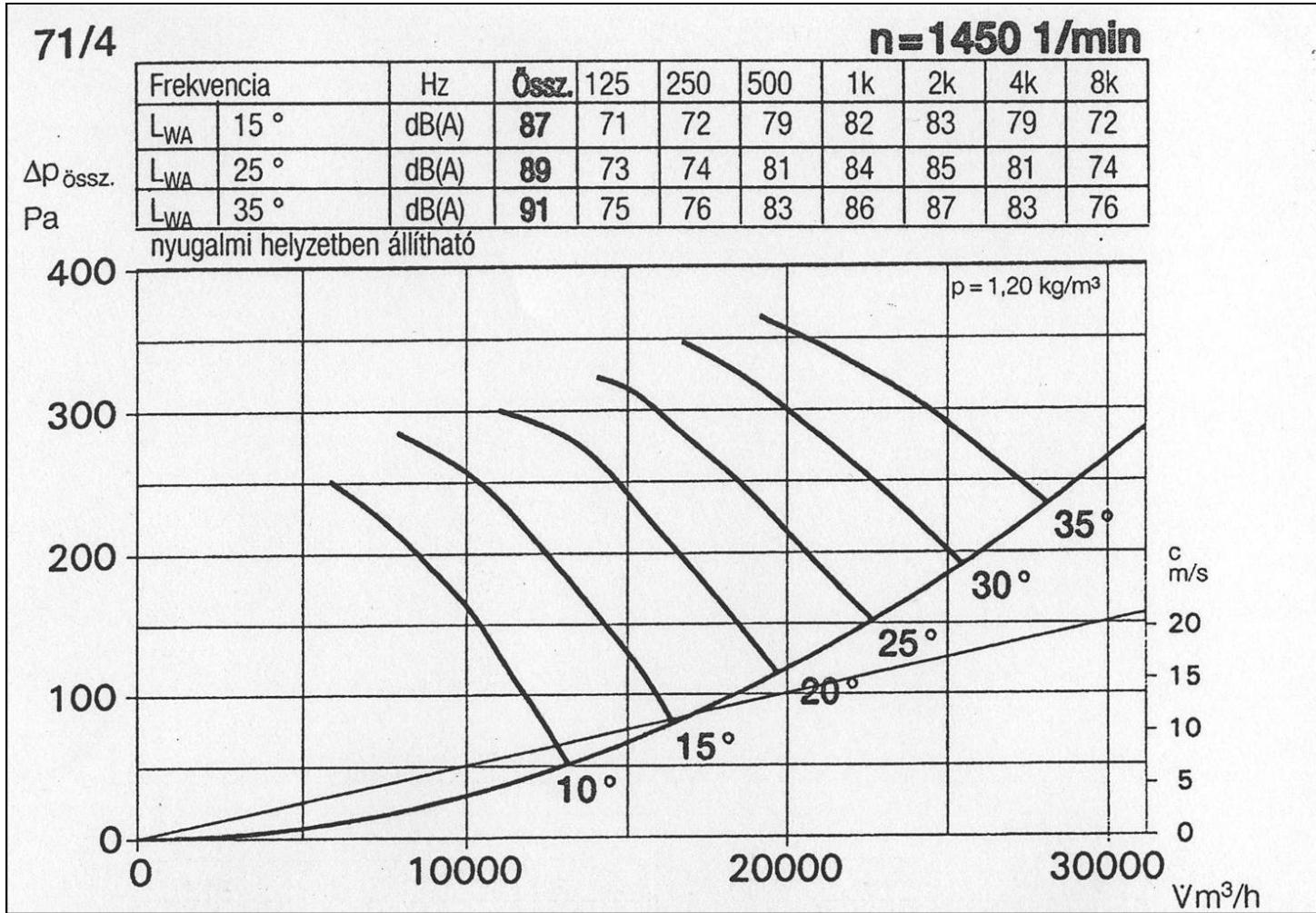


$$\Delta p_t = \left(\rho \frac{v_2^2}{2} + p_0 \right) - p_0 = \rho \frac{v_2^2}{2} \quad \Delta p_{st} = \Delta p_t - \rho \frac{v_2^2}{2} = 0$$



The static pressures are different on the two sides!

1.7. Characteristic curve: an example



1.8. Dimensionless characteristics, comparison

User demands:

$$\Delta p_t, (\Delta p_{st}), q_V, P_{overall}$$

Machine characteristics:

$$D \text{ (rotor outer diameter)}, n$$

Fluid characteristics:

$$\rho, \nu$$

For comparison of various machines: $u_t = D \pi n$

Total pressure coefficient:

$$\Psi_t = \frac{\Delta p_t}{\frac{\rho}{2} u_t^2}$$

Static pressure coefficient:

$$\Psi_{st} = \frac{\Delta p_{st}}{\frac{\rho}{2} u_t^2}$$

Flow coefficient: $\Phi = \frac{q_v}{A_{char} u_t}$

Power coefficient: $\lambda = \frac{P_{overall}}{\frac{\rho}{2} u_t^2 A_{char} u_t} = \frac{\eta_{overall}}{\frac{\rho}{2} u_t^2 A_{char} u_t} = \frac{\Psi_t \Phi}{\eta_{overall}}$

Reynolds number: $Re = \frac{u_t \ell}{\nu}$

