

Numerical schemes for compressible flows

- We can assume, that the state of a computational element is determined by its neighbors.
- That way, the solution of large algebraic systems can be avoided.
- The price to be paid: acoustic waves need to be resolved, that is, the time step size is limited.























	$\frac{\partial a}{\partial t} + u \frac{\partial a}{\partial x} + \frac{\gamma - 1}{2} a \frac{\partial u}{\partial x} = 0 \tag{1}$
	$\frac{\gamma - 1}{2}\frac{\partial u}{\partial t} + \frac{\gamma - 1}{2}u\frac{\partial u}{\partial x} + a\frac{\partial a}{\partial x} = 0 $ (2)
(1) + (2)	$\frac{\partial}{\partial t} \underbrace{\left(a + \frac{\gamma - 1}{2}u\right)}_{\alpha} + (u + a) \frac{\partial}{\partial x} \underbrace{\left(a + \frac{\gamma - 1}{2}u\right)}_{\alpha} = 0$ $\frac{\partial \alpha}{\partial t} + (u + a) \frac{\partial \alpha}{\partial x} = 0 \qquad \alpha = \text{const. in the direction of } C_* = dx/dt = u + a.$
(1) - (2)	$\frac{\partial}{\partial t} \underbrace{\left(a - \frac{\gamma - 1}{2}u\right)}_{\beta} + (u - a) \frac{\partial}{\partial x} \underbrace{\left(a - \frac{\gamma - 1}{2}u\right)}_{\beta} = 0$ $\frac{\partial \beta}{\partial t} + (u - a) \frac{\partial \beta}{\partial x} = 0 \qquad \beta = \text{const. in the direction of C}_{z=dx/dt=u-a}$













