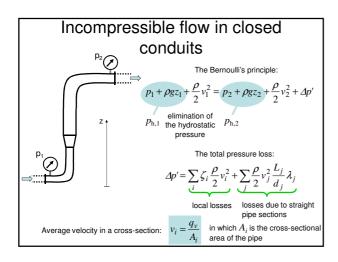
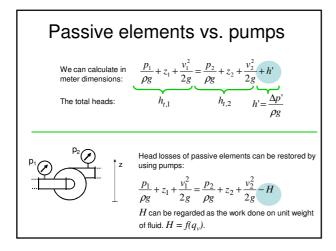
8. Hydraulics

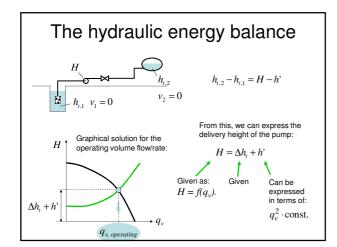
Dr. Gergely Kristóf Dept. of Fluid Mechanics, BME April, 2014.



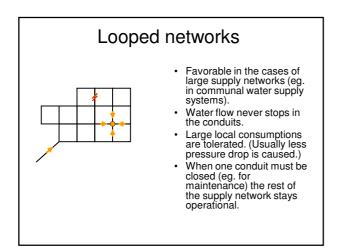


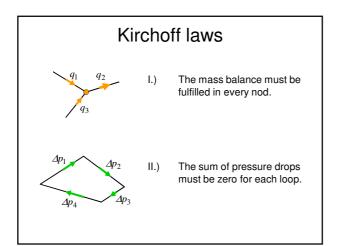


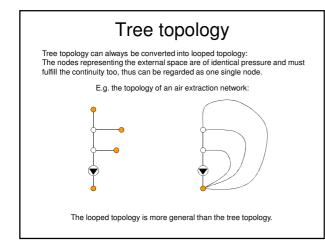




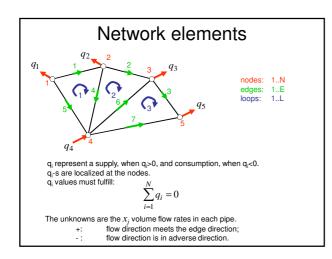




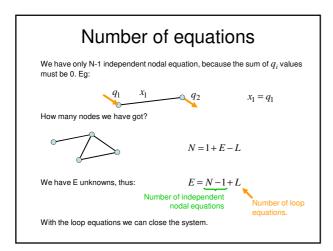




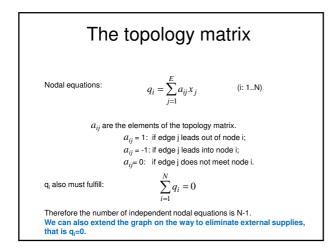




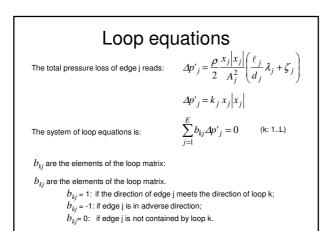








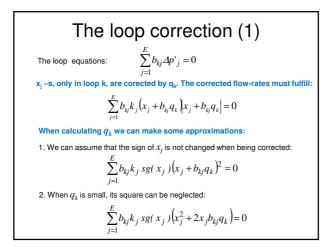




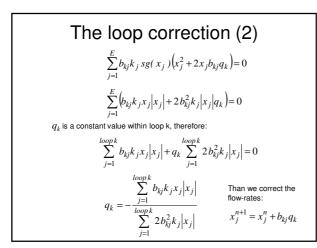
The Cross method

An easy to implement iterative solution method for looped networks.

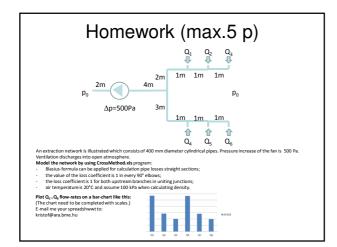
- Set the volume flow rates on the way to fulfill the nodal equations. 1. Eg. we set $x_i = 0$.
- Correct the flow rates of all edges within loop k by adjusting their x_j values with a q_k loop correction flow rate. (Correct only one loop at a trace) 2. Values with a q_k loop correction flow rate. (Correct only one loop at a time.) This method does not violate the validity of the nodal equations. Apply the loop corrections sequentially on each loop. We always spoil the pressure balance of the neighboring loops at some extents.
- 3.
- Repeat the corrections in cycles. 4.













Newton-Raphson method with direct solution

Independent loop corrections do not give a convergent solution in complex cases, so we need to solve the linear system directly for the whole flow rate correction vector.

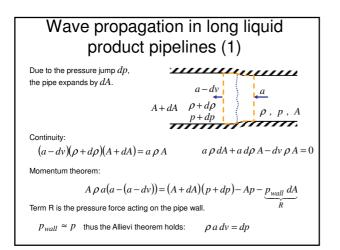
The flow rate of the j^{a_h} conduit is updated by taking into account q_m values of every loop:

$$x_j^{n+1} = x_j^n + \sum_{m=1}^{L} b_{mj} q_m$$

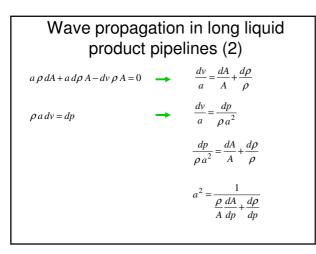
With this assumption, the loop-equation for the k^{th} loop reeds:

$$\sum_{j=1}^{E} \left(b_{kj} k_j x_j^n | x_j^n | + 2 b_{kj} k_j | x_j^n | \sum_{m=1}^{L} b_{mj} q_m \right) = 0$$

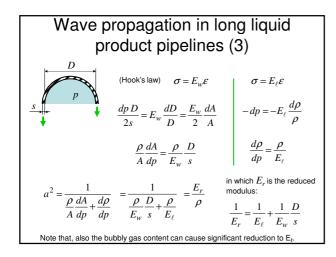
This formulates a system of L (k:1..L) equations for the unknown q_m (m:1..L) values can be solved by any direct solution method, e.g. by Gauss-Jordan method.













Problem #8.1

A) Compare the wave celerity in still water with those in a pipeline of given geometrical parameters:

Pipe diameter: 500 mm, Wall thickness: 10 mm, E_{water} : 2.0 x 10⁹ Pa, E_{steal} : 2.1 x 10¹¹ Pa.

B) For which value of s/D ratio is the difference in sound speeds equal to 5% of the sound speed in clear water?

To the solution

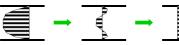
Unsteady flow in liquid product
pipelines
Continuity equation for constant nominal cross-section pipes:
$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x} (\rho v) = 0$$
The equation of motion:
$$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + f$$
f denotes the force on unit mass of fluid due to wall friction:
$$f = \frac{1}{\rho} \frac{\Delta p'}{\Delta x}$$
for turbulent flow, we can state:

$$\Delta p' = -\frac{\rho}{2} v |v| \frac{\Delta x}{D} \lambda$$
, thus $f = -\frac{\lambda}{2D} v |v|$

Pipe friction coefficient for unsteady flows

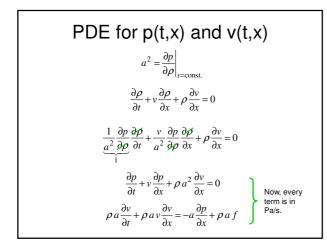
For periodical flows of sinusoidal time dependence λ can be specified as a function of Re and St = f D / v.

When the pressure gradient changes direction:

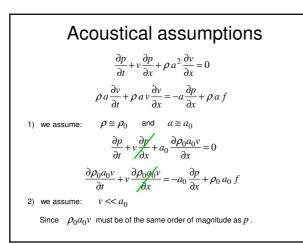


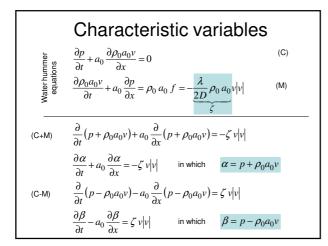
Unsteady λ values are usually greater than the steady values due to the continuous refreshment of the boundary layer. For laminar flow even an analytical solution can be found in the literature.

For turbulent flows λ can be identified on the basis of resonance experiments carried out in closed pipes. According to our own measurements, λ fell in the range of 0.02-0.04 (for some experiments in the ranges of Re:10^4-10^5 and St:0.005-0.02).

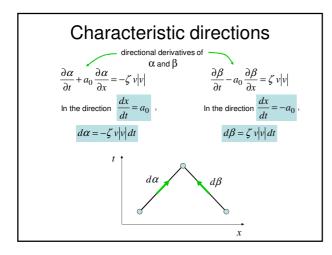




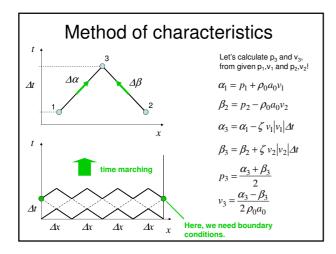




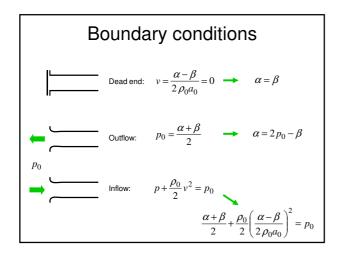




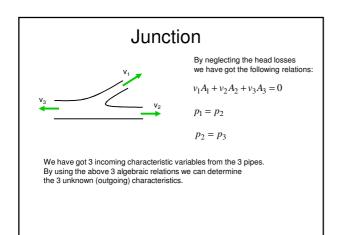


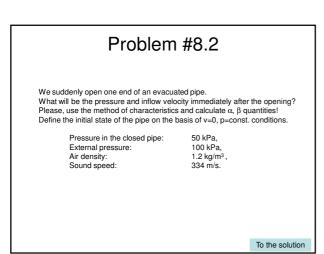












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