

MEASUREMENT 11.

Examination of flows around bodies

1. OBJECTIVES OF THE MEASUREMENT, PRACTICAL RELEVANCE

The main objective of the measurement is the analysis of the flow around bodies with different profile shapes (square pillar, circular pillar and symmetric airfoil) by the visualization of the flow field. The secondary objectives are the determination of the pressure distribution around the bodies through measurements, and the investigation of the connection between the developed flow pattern and the pressure distribution along the wall. In the laboratory report you should compute the drag coefficients based on the pressure distribution, and compare the flow patterns around the different shaped bodies.

In practice, we often need to know the characteristics of the flow field developing around bodies. The most important of these are the velocity and pressure distributions and the aerodynamical forces acting on the body. Knowing these is very important, for example in vehicle and aircraft design, and in the static investigation of buildings. A quite interesting phenomenon, which can be investigated, is the periodic fluctuation around bodies, where both the velocity and pressure field fluctuate. Therefore, the aerodynamical forces fluctuate as well, which may cause problems, if the frequency of the fluctuation is close to the mechanical resonance frequency of the body. In such cases, the amplified fluctuation may cause mechanical damage to the structure. For that very reason, the dynamical examination of the flow pattern around long bodies is also important when statically examining them.

This laboratory examination demonstrates the basic concepts and practices of this topic.



2. Description of the measurement facility

The measurement facility, which can be used to investigate plane channel flows, contains two main parts. The first part is a miniature wind tunnel, which provides a uniform inlet velocity profile, and the second part is the adjustable measuring section. The complete measurement set-up can be seen in Fig. 1. Its components listed in the order following the flow path are the following:



Figure 1. The schematic of the device

- 1. Standard inlet orifice plate for measuring the flow rate.
- 2. Air intake nozzle.
- 3. Pressure tap after the inlet orifice plate, which is connected to the proper tap (in this case that is the tap denoted by "-") of the pressure transducer by a thin rubber tube. From the measured pressure the volume flow rate can be calculated.
- 4. Two channel digital manometer.
- 5. Radial fan driven by a triphase asynchronous motor.
- 6. Flow straightener.
- 7. The measurement section provides the means for assembling the different channel geometries for the investigations. The almost uniform flow from the straightener is directly

fed into the adjustable measurement section. The measurement section is bounded on the bottom side by a cork covered base plate (the flow visualization flags (8) can be stuck into this plate). The top of the channel consists of a transparent plexiglas plate, which can be opened. The sides consist of two adjustable plates.

- 8. Flow visualization flags.
- 9. Side walls with pressure taps on the surface.

Beside the previously described measuring facility other auxiliary devices are also needed for the measurement (e.g. barometer, thermometer, tape measure etc.). These are also provided in the laboratory.

(Note: The base and the top plates are parallel planes to each other and the sidewalls are perpendicular to them in every cross section of the channel. Therefore, by neglecting the displacement effect of the boundary layer, it can be assumed that the fluid particles are not deflected perpendicularly to the bottom and top boundary. Generally speaking, in this direction the flow variables are changing with a much smaller rate than along the other two dimensions of the measurement section. This is the observation which gives us the opportunity to investigate relatively simple two dimensional flows using this facility.)

3. Detailed description of the measurement task, basic aspects of the tests and postprocessing

The extensive examination of the topics outlined in section 1. would require a long amount of time. Within the confines of this lab measurement, three types of basic investigations have to be completed

- A. Investigation of the flow around a body with circular cross section.
- B. Investigation of the flow around a body with a square cross section.
- C. Investigation of the flow around a body with a symmetric airfoil cross section

3.1. Investigation of the flow pattern in the channel using a flow visualization technique

The first step is to set-up the required measurement section by placing the proper side wall elements onto the base plate, and placing the measured object in the proper position in the channel. Following this, the flow visualisation flags need to be stuck into the base plate in the free-stream flow of the channel. The visualisation flags are pins with a 30-35mm length soft and fluffy thread mounted to the upper part of the pins. Taking into consideration the nature of the process, the flags need to be placed with 20-90 mm spacing. It is evident that the flags should be placed densely in the places where the flow changes significantly within a short distance and sparsely where the flow is undisturbed. It is advisable to place the threads on the pins approximately at the mean of the channel height. After the flow is started the flags turn into the local flow direction. If the flags are properly placed, the flow pattern in the channel is visualized by the many small threads. In order to document the observations, a freehand sketch or a photograph should be made of the flags. The sketch should focus on the sudden direction changes and separations which appear in the flow. It is practical to separately denote the contours of the separation bubbles on the drawings.

At the inlet section of the channel a Pitot-static probe, otherwise known as a Prandtl probe, velocity measurement should be done in order to check the uniformity of the inlet velocity profile and to calculate the approximate value of the average velocity and compare it to the value computed from the inlet orifice plate. The average velocity should be determined based on the rules of the point to point Prandtl-probe measurement. In the inlet section the measurement points should be evenly distributed with 7-15 mm of spacing. Results should be presented in a table and a chart along with the average velocity values computed from the inlet orifice plate measurements.

3.2. Measurement of the pressure distribution on the body

Beside the velocity field, another important characteristic property which is present in the fluid flow is the pressure distribution. The pressure changes are in correlation with the changes in the flow pattern. Many velocity and flow rate measurement devices apply this observation (e.g. Prandtl-probe, Venturi tube).

In the present experimental exercise the pressure distribution on the surface of an object placed in the flow will be examined. Following this, the connection between the pressure distribution measured on the object and the velocity distribution realized in the measurement section needs to be determined. The pressure distribution on the surface of the object can be examined by using the pressure taps on the surface of the object, and the digital manometer. One of the taps on the manometer needs to be connected to the pressure tap of the object which is to be examined, and the other needs to be connected to the pressure tap on the wall of the channel which is close to the inlet of the channel. In this way we can measure the pressure on the entire surface of the object with respect to the static pressure in the channel. Taking into consideration the equipment which is available for the measurement, the measurements on the cylinder should be executed every 5° , while the pressure taps on the square figure are distributed evenly across the cross-section. The results of the measurements should be shown in a diagram. Having acquired the pressure distribution and the flow maps, the connections between them should be investigated, with the found results being included in the report.

3.3. Determination of the drag force, the drag coefficient and pressure coefficient

During the analyses of the data, you should calculate the pressure coefficient from measured pressure values. Diagrams are required in the lab report for both the pressure difference values and the pressure coefficient values as a function of either the position or the angle of the object. The pressure coefficient can be calculated as follows:

$$c_{p,i} = \frac{p_i}{\frac{\rho_{air}}{2}v^2}$$
 where:

$$c_{p,i} \quad [-] \qquad \text{pressure coefficient}$$

$$p_i \quad [Pa] \qquad \text{pressure from the}$$

$$\rho_{air} \quad [kg/m^3] \qquad \text{fluid density}$$

$$v \quad [m/s] \qquad velocity$$

The experimental methods described in sections 3.1 and 3.2 can be used to make a detailed analysis of the flow around a body. Usually though, in the everyday engineering practice, it is not necessary to use such a detailed description. In such cases it is beneficial to calculate the drag force and to use only the dimensionless drag coefficient.

The drag force can be calculated from the pressure distribution, by dividing the surface of the body into sections according to the positions of the pressure measurement points around the body, thus the measurement points will be in the centers of the sections. The total force of the body, which originates from pressure, can be calculated from the sum of the forces on the different sections:

$$\underline{F} = \sum_{i=1}^{n} \underline{F}_{i} = \sum_{i=1}^{n} p_{i} A_{i}(-\underline{e_{n}}) = \sum_{i=1}^{n} p_{i} h_{i} L(-\underline{e_{n}}) \quad \text{where:}$$

<u>F</u>	[N]	total force from the pressure
n	[pieces]	number of sections/ points
$\underline{F_i}$	[N]	force of the i-th section
\mathbf{p}_{i}	[Pa]	pressure of the i-th section
A_i	$[m^2]$	the area of the i-th section
$\underline{e_n}$	[-]	unit vector in normal direction of the i-th section
h _i	[m]	the width of the i-th section
L	[m]	the height of the i-th section

The next equations explain the calculation of the drag force for circular cross-sections

 $F_{x} = \sum_{i=1}^{n} F_{ix} = \sum_{i=1}^{n} p_{i} L2R(-1) \sin\left(\frac{\Delta \Phi_{i}}{2}\right) \cos \Phi_{i}$ and

$$F_{y} = \sum_{i=1}^{n} F_{iy} = \sum_{i=1}^{n} p_{i} L2R(-1) \sin\left(\frac{\Delta \Phi_{i}}{2}\right) \sin \Phi_{i}$$

, where the variables can be seen in the figure (fig. 2)



Having these components, we can derive any component of the total force from the results. This can be, for example, the lift force and the drag force, which are customary in aerodynamics. These are the components, which are parallel to the main stream (drag force (F_d)) and perpendicular to it (lift force (F_l)).

In the present investigation the focus is on the drag force and the drag coefficient. The drag coefficient can be computed as follows:

$$c_e = \frac{F_d}{\frac{\rho_{air}}{2}v^2 A_o}$$
 where:

F_d	[N]	is the drag force.
$\rho_{air} = \frac{p_0}{RT_t}$	[kg/m ³]	fluid density
p_0	[Pa]	atmospheric pressure
R=287	[J/kg/K]	specific gas constant
T _t	[K]	laboratory temperature
A ₀	$[m^2]$	cross-sectional area of the body perpendicular to the flow
$v = \frac{q_v}{A}$	[m/s]	velocity
A	$[m^2]$	free cross-section of the channel
q_v	[m ³ /s]	volume flow rate

The volume flow rate q_v can be measured with the inlet orifice plate mounted at the beginning of the suction tube. It is assumed that the fan intake occurs through the orifice and discharges into the ambient fluid only at the channel exit. This means that the sealing in system is perfect and since the density is constant, the volume flow rate does not change in the device.

The volume flow rate can be determined by the inlet orifice plate as follows. The relative pressure as compared to the atmospheric pressure Δp_{mp} is measured at the tap following directly after the orifice plate at the beginning of the suction tube. The volume flow rate q_v can be computed from Δp_{mp} with the following expression:

$$q_{v} = \alpha e \frac{d^{2}\pi}{4} \sqrt{\frac{2\Delta p_{op}}{\rho_{air}}}$$

, where:

 $q_v \left[m^3/s \right]$ is the volume flow rate through the orifice

 α [-] is the contraction ratio, which depends on the area ratio of the orifice and the tube and on the Reynolds number. The value of α is determined from experimental investigations and it has been summarized in handbooks. In this measurement the contraction ratio is approximately 0.6.

 ε [-] is the expansion number, which is assumed to be 1 in the circumstance of small pressure variation through the system, such as in this measurement.

d [m] is the diameter of the orifice plate.

 Δp_{op} [Pa] is the pressure loss on the orifice plate.

$$\rho_{air}$$
 [kg/m³] is the density of the fluid.

A detailed description of the volume flow rate measurement with an orifice plate can be found in [2] on pages 38-43.

Table 1. contains informative details regarding the drag coefficient of three-dimensional bodies as a function of the flow direction

3.4. The lab report

3.4.1. The lab report must contain the following:

- $v_x(y)$ velocity profiles for the inlet and outlet cross sections of every measurement, x being the main flow direction.

- Distribution of the static pressure coefficient (c_p) on the bodies surface as a function of the angle $c_p(\phi)$ (cylinder) and as a function of the range $c_{pst}(x)$ (prismatic body), for every measurement set-up.
- The flow field around the body should be demonstrated using the flow visualization flags.

3.4.2. Error calculation for the measurement

Error calculations (absolute and relative error) should be carried out for the calculated value of the drag coefficient. The results should be demonstrated on separate diagrams, one showing the relative error, and another showing the values of the drag coefficient with error bars to showing the absolute error.

$$c_{e} = \frac{\sum p_{i}A_{i}}{\frac{\rho_{air}}{2}\left(\frac{q_{v}}{A}\right)^{2}A_{0}} \qquad \qquad \delta c_{e} = \sqrt{\sum_{i=1}^{n} \left(\delta X_{i}\frac{\partial c_{e}}{\partial X_{i}}\right)^{2}} \qquad \qquad \frac{\delta c_{e}}{c_{e}} = 2$$

where X_i is the value of measured quantities

quantities	errors
$X_1 = p_0$	$\delta p_0 = 100 \ Pa$
$X_2 = T_0$	$\delta T_0 = 1K$
$X_3 = \Delta p$	$\delta p=2 Pa$
$X_4 = \Delta p_{op}$	$\delta p=2 Pa$

Remember that during the labs:

- Before turning any measurement device on or in general during the lab, make sure that safe working conditions are ensured. The other participants have to be warned of the starting of the machines and of any changes that could endanger the members of the lab.

- The atmospheric pressure and room temperature should be recorded before and after every measurement.
- The measurement units and other important factors (e.g. data sampling frequency, date of calibration) of every recorded value of the applied measurement devices should be recorded.
- Type and construction number of the applied measuring instrument should be included in the final report.
- Checking and harmonizing of the units of the recorded values with those used in further calculations.
- Manometers should be calibrated if necessary.
- The measurement ports of the pressure meter should be carefully connected to the correct pressure ports of the instrument.
- If inlet or outlet tubes are to be assembled with fans, connections should be airtight as escaping/entering air can significantly modify the measurement results.

Bibliography:

[1] Lajos Tamás: Az áramlástan alapjai, Műegyetemi Kiadó 2004

BODY SHAPE AND FLOW DIRECTION (3D BODIES)	C _D [-]	BODY SHAPE AND FLOW DIRECTION (3D BODIES)	C _D [-]
→ □	1.05	\rightarrow	1.55
+	2.05	+	2.01
\rightarrow	1.42	\rightarrow	2
\rightarrow	0.38	\rightarrow	1.55
\rightarrow	1.17	\rightarrow	2.3
\rightarrow	0.42	→(1.2
\rightarrow	0.04	→ <u></u>	1.17
		\rightarrow	2.05

Table 1. Drag coefficients for a range of $Re=10^3-10^5$